

中国科学院上海天文台
Shanghai Astronomical Observatory, Chinese Academy of Sciences

ClUsteR strong Lens modeling for the Next- Generation observations (CURLING)

The Bias from Point-like Multiple Image Approximation



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OUTLINE

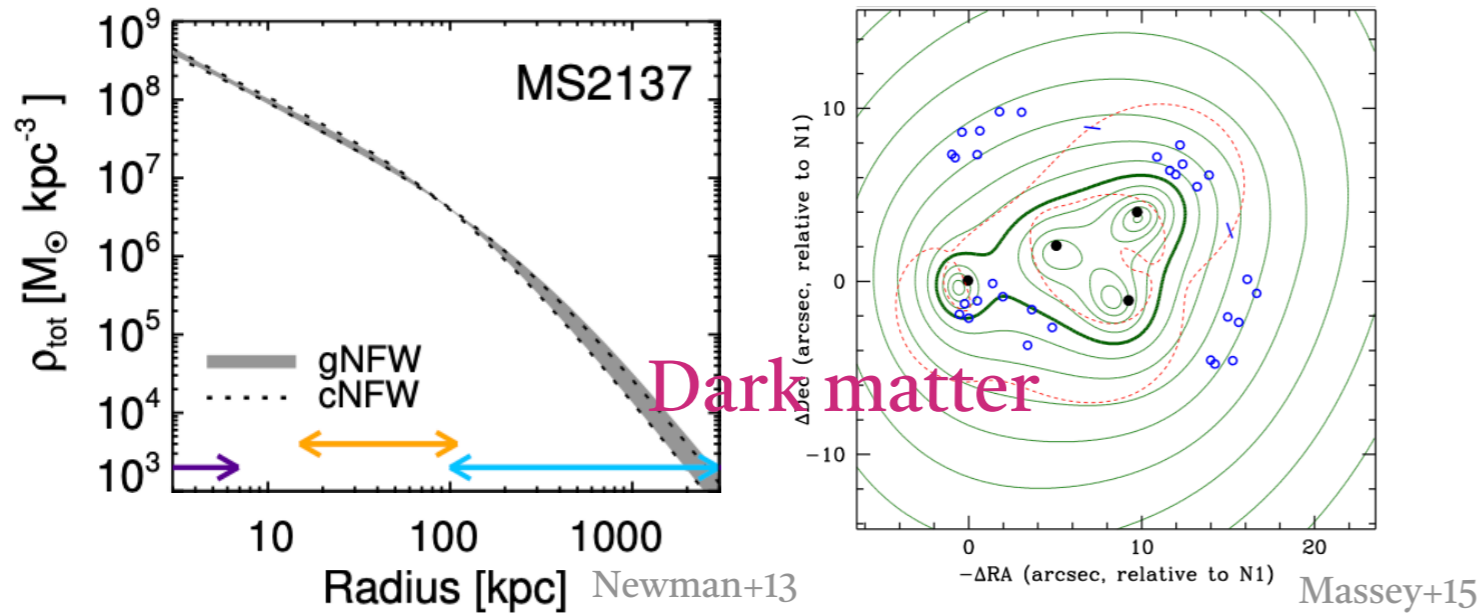
I. Basics

II. The bias from point-like multiple image approximation

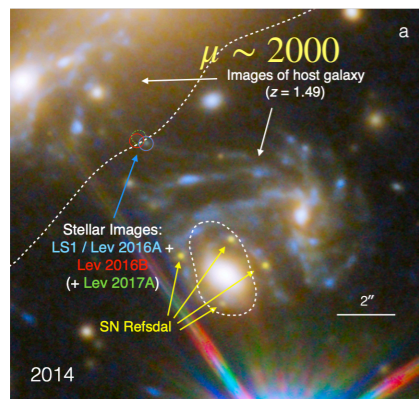
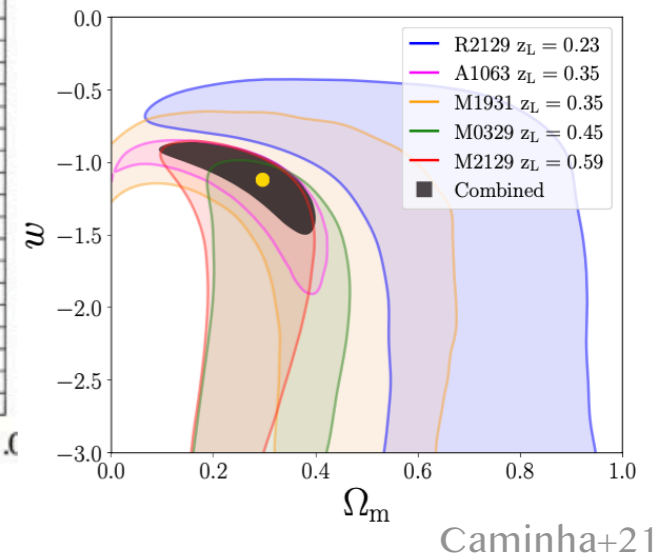
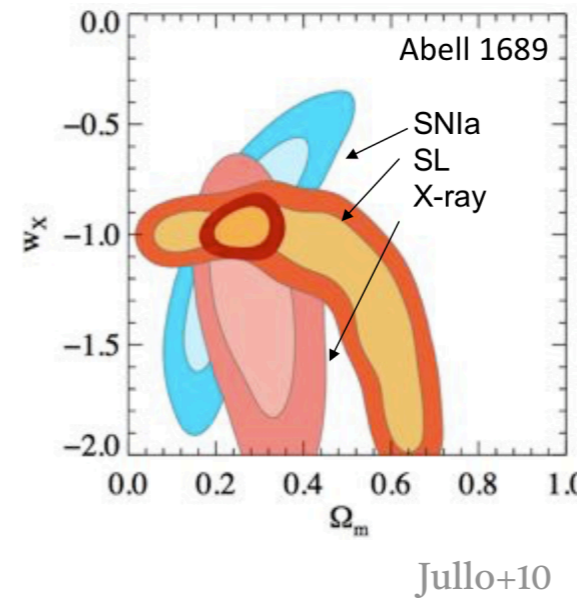
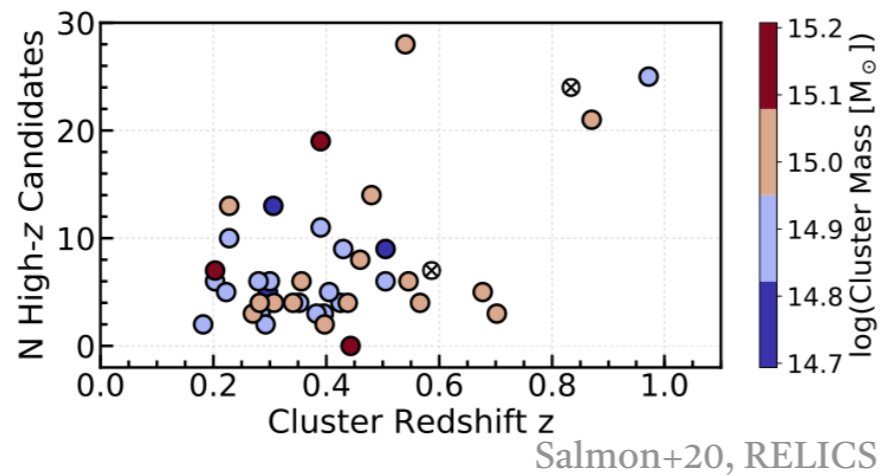
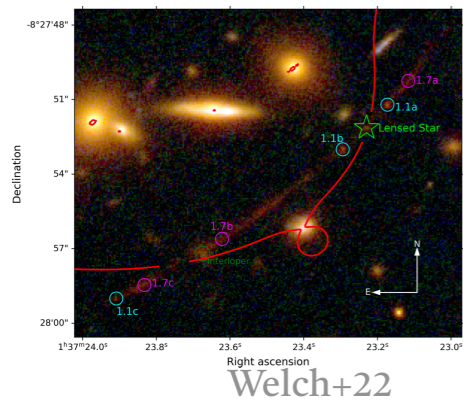
III. Solution: A pixelated method

IV. Next steps

I. Basics: cluster strong lensing



- ~ 1 SL cluster-lens per ~ 10 sq. deg:
potentially ~ 2000 to study,
only ~ 200 identified today,
nearly ~20 with a good mass model
(taken from Jean-Paul's talk, 2011)



Kelly+18

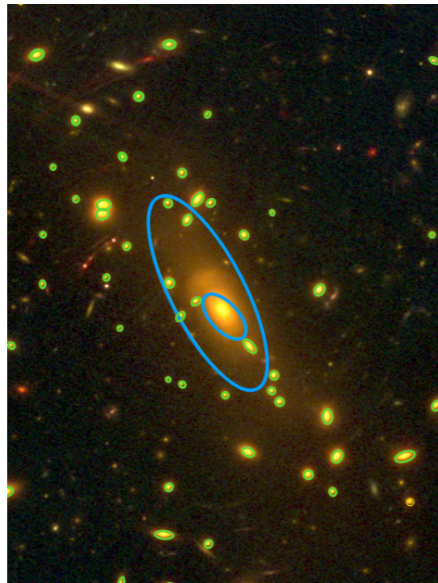
High-z Universe

Cosmography

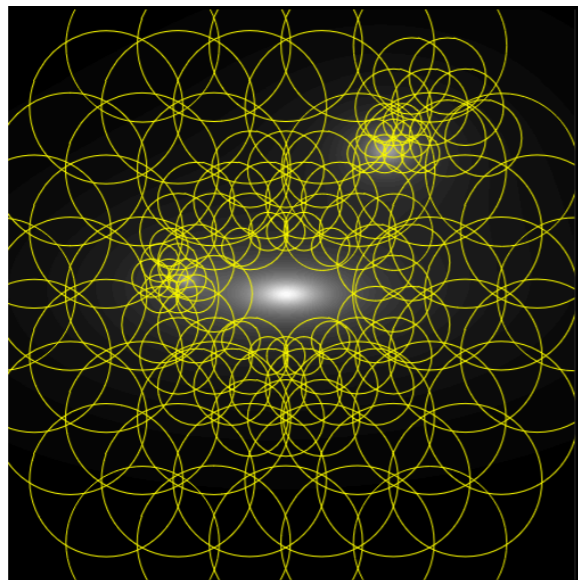
I. Basics: cluster strong lensing

Parametric

$$\phi_{\text{tot}} = \sum_i \phi_{c_i} + \sum_j \phi_{p_j}$$



Non-parametric



Strong lens modeling: algorithms

Package	Model
gravlens / lensmodel	Para
Lenstool	Para/Non-Para
LensPerfect	Non-Para
glafic	Para
PixeLens	Non-Para
SimpLens	Non-Para
Lensview	Non-para
GRALE	Non-Para
GravLensHD	Para
G-Lens	Para
Gravitational Lensing	Para
lens	Para/Non-para
MOWGLI	-

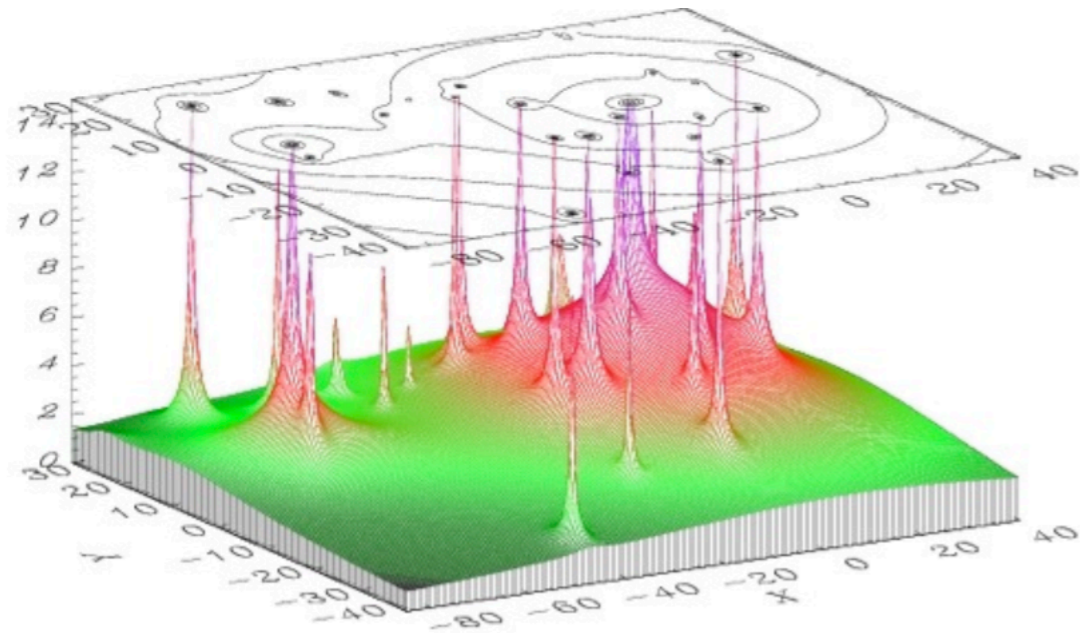
II. The bias from point-like multiple image approximation

Parametric lens modeling

- 🕒 Constraints (position, redshift, **shape, flux**)
- 🕒 Model parameterization
 - Large scale clumps: dark matter halo, gas
 - Small scale substructures: galaxy subhaloes
- 🕒 Model optimization **Too complex!**

Systematics from observational side:

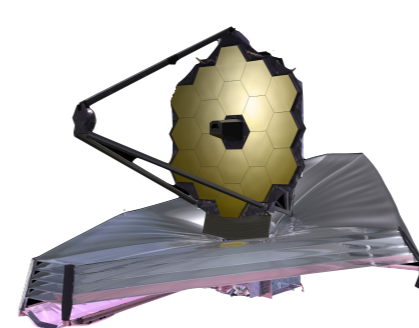
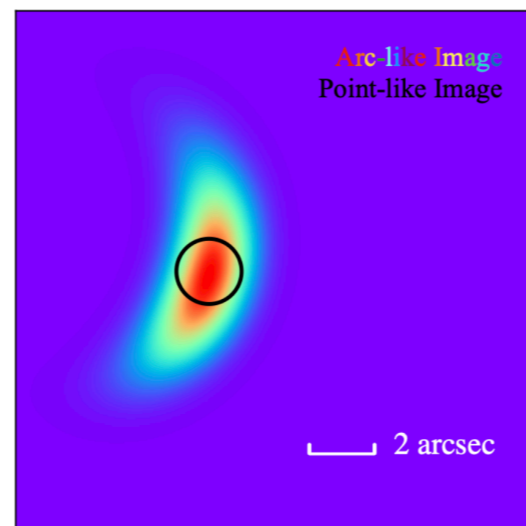
- *scaling relation,*
- *line-of-sight halos,*
- *model assumption,*
- *astrometric errors*
- ...



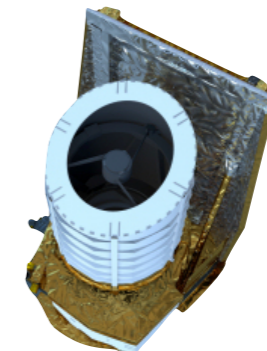
Kneib+1996

The bias

$$\chi_i^2 = \sum_{j=1}^{n_i} \frac{[\theta_{\text{obs}}^j - \theta^j(\mathbf{p})]^2}{\sigma_{ij}^2}$$



JWST



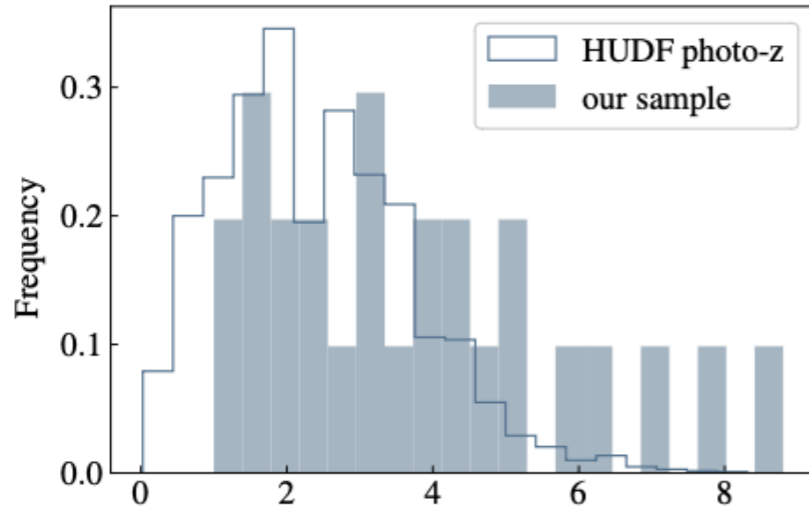
Euclid



CSST

II. The bias from point-like multiple image approximation

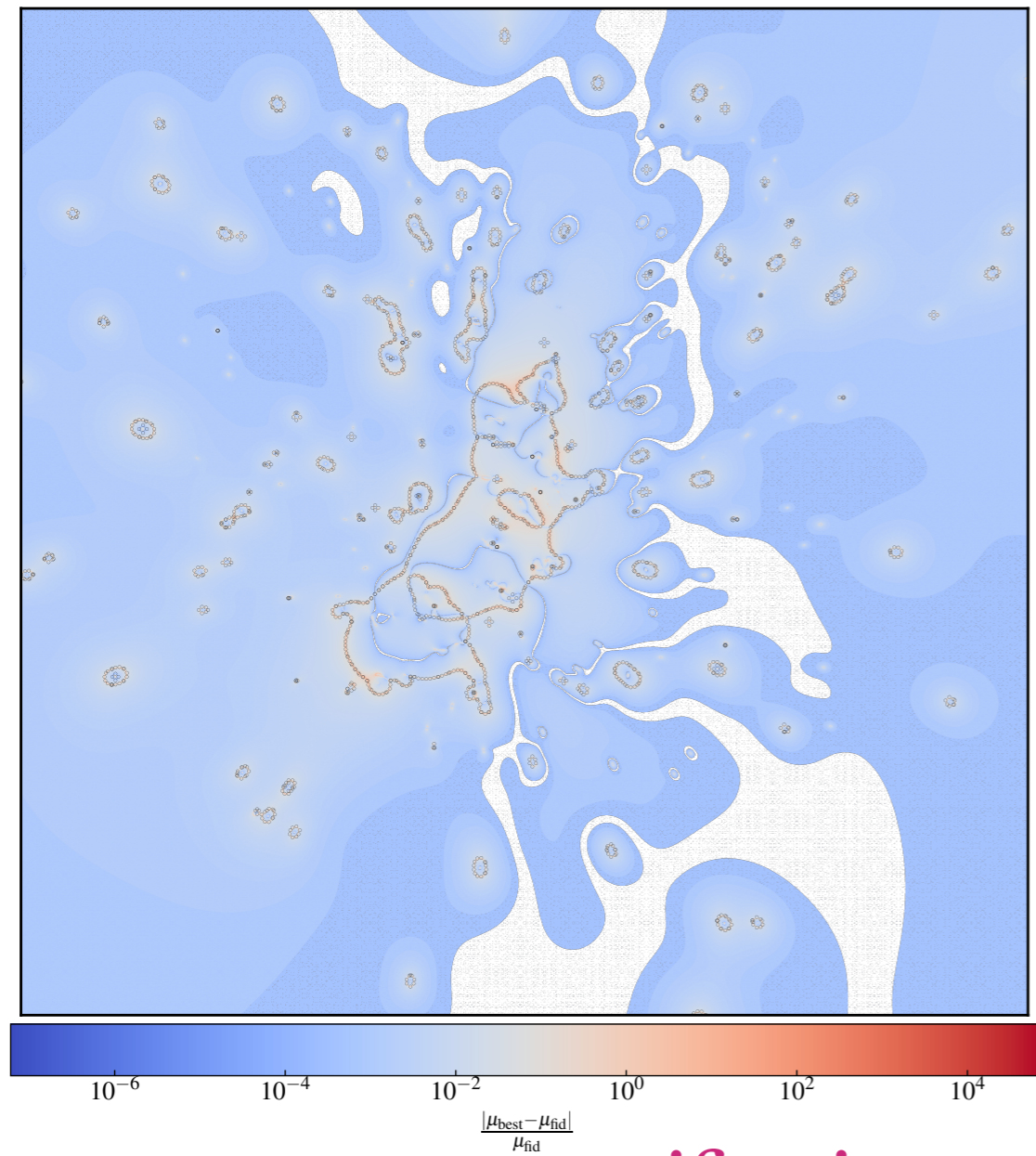
Test on simulated
strong lensing clusters:
extracted from
Hubble Frontier Fields



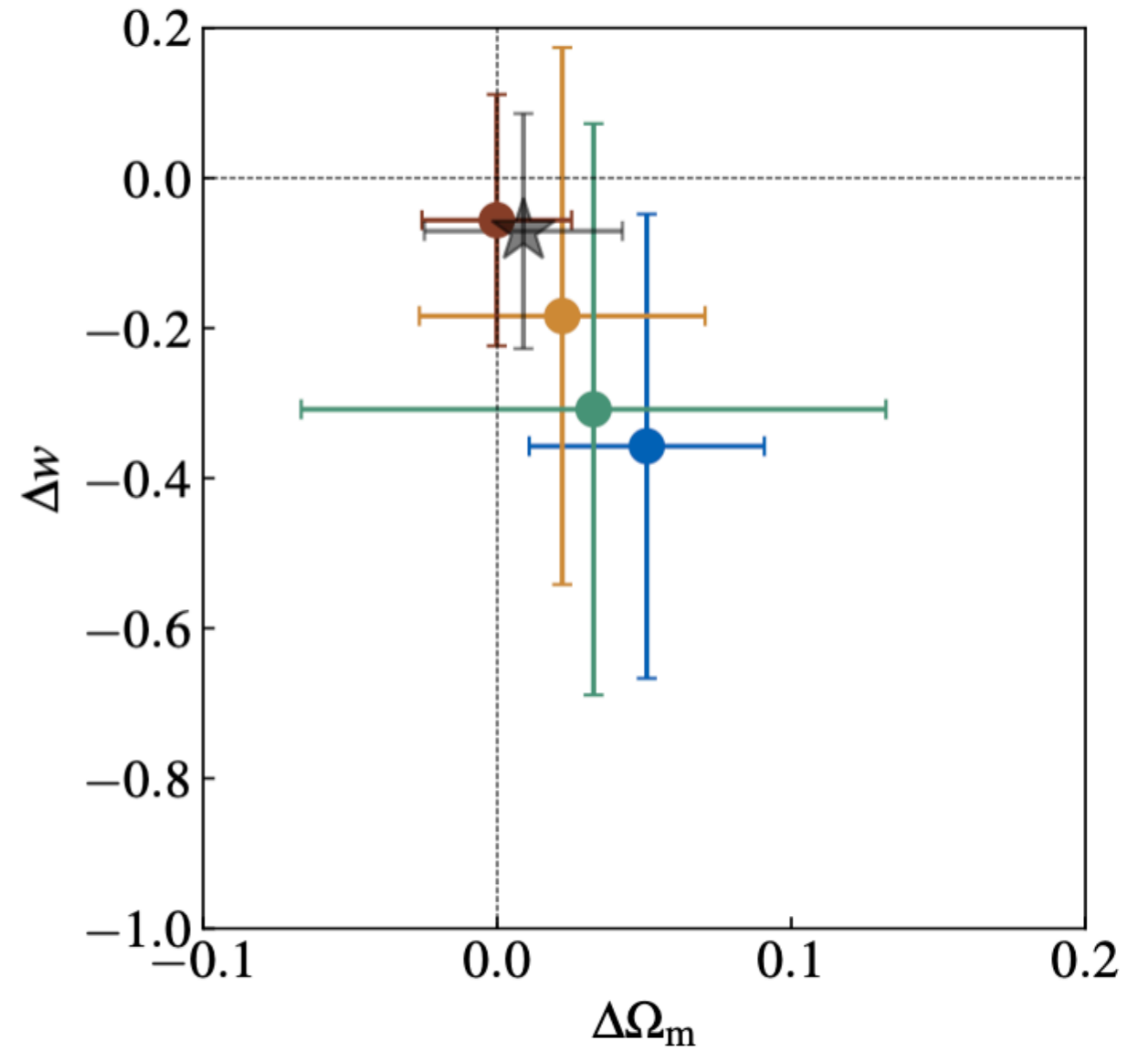
Source redshift distribution

Component	$\Delta\alpha$ ["]	$\Delta\delta$ ["]	e	θ [deg]	r_{core} [kpc]	r_{cut} [kpc]	σ [km/s]
MACS0416-like, $z = 0.35$ $N_s = 26, z_{s,\text{toy}} = \{1.6, 3.5, 6.1\}$							
Cluster Halo 1	-0.22	0.06	0.81	143.14	37.39	987.95	615.06
Cluster Halo 2	22.67	-34.27	0.89	136.49	26.26	987.95	466.55
Cluster Halo 3	-32.45	8.80	0.00	0.00	34.23	987.95	308.96
Cluster Halo 4	22.80	-48.15	0.76	122.43	66.73	987.95	707.09
Perturber 1	31.96	-65.55	0.00	0.00	4.94	274.19	76.82
Perturber 2	13.34	2.62	0.60	-45.59	4.94	65.12	106.11
scaling relations	$N(\text{gal}) = 212$	$m^{\text{ref}} = 17.02$	$r_{\text{core}}^{\text{ref}} = 0.15$	$r_{\text{cut}}^{\text{ref}} = 15.00$	$\sigma^{\text{ref}} = 210.00$		
A2744-like, $z = 0.4$ $N_s = 22, z_{s,\text{toy}} = \{1.5, 2.4, 3.8\}$							
Cluster Halo 1	-1.42	0.55	0.59	91.39	28.65	1500.0	515.54
Cluster Halo 2	-17.85	-15.22	0.40	53.89	34.12	1600.0	632.73
Ext. Clump 1	99.49	85.97	0.00	0.00	1.3	800.0	111.28
Ext. Clump 2	138.28	99.87	0.00	0.00	1.4	800.0	372.13
Ext. Clump 3	24.23	155.84	0.00	0.00	1.4	800.0	294.63
BCG-N	0.0	0.0	0.28	133.03	1.3	800.0	208.77
BCG-S	-17.95	-20.05	0.74	26.29	0.17	178.47	308.02
scaling relations	$N(\text{gal}) = 223$	$m^{\text{ref}} = 17.34$	$r_{\text{core}}^{\text{ref}} = 0.15$	$r_{\text{cut}}^{\text{ref}} = 19.52$	$\sigma^{\text{ref}} = 252.66$		
MACS1206-like, $z = 0.45$ $N_s = 25, z_{s,\text{toy}} = \{1.9, 4.2, 5.7\}$							
Cluster Halo 1	-1.40	0.14	0.72	19.76	35.22	1151.89	748.96
Cluster Halo 2	9.20	3.63	0.46	116.69	77.60	1151.89	662.94
Ext. Clump 1	-28.87	-6.83	0.33	-25.16	70.94	1151.89	501.28
scaling relations	$N(\text{gal}) = 258$	$m^{\text{ref}} = 17.19$	$r_{\text{core}}^{\text{ref}} = 0.15$	$r_{\text{cut}}^{\text{ref}} = 15.0$	$\sigma^{\text{ref}} = 210.0$		
AS1063-like, $z = 0.5$ $N_s = 23, z_{s,\text{toy}} = \{2.4, 3.3, 4.3\}$							
Cluster Halo 1	1.44	-0.73	0.63	-38.91	111.26	1220.84	1165.26
Cluster Halo 2	-48.60	26.26	0.01	0.00	30.52	1220.84	213.01
Ext. Clump 1	18.90	-73.36	0.80	-162.05	8.55	1155.16	355.93
BCG	-18.05	13.47	0.13	-27.80	221.73	2070.29	442.57
Perturber	0.20	-1.24	0.34	-15.49	88.11	610.42	249.68
scaling relations	$N(\text{gal}) = 222$	$m^{\text{ref}} = 16.18$	$r_{\text{core}}^{\text{ref}} = 0.15$	$r_{\text{cut}}^{\text{ref}} = 15.0$	$\sigma^{\text{ref}} = 210.0$		

II. The bias from point-like multiple image approximation

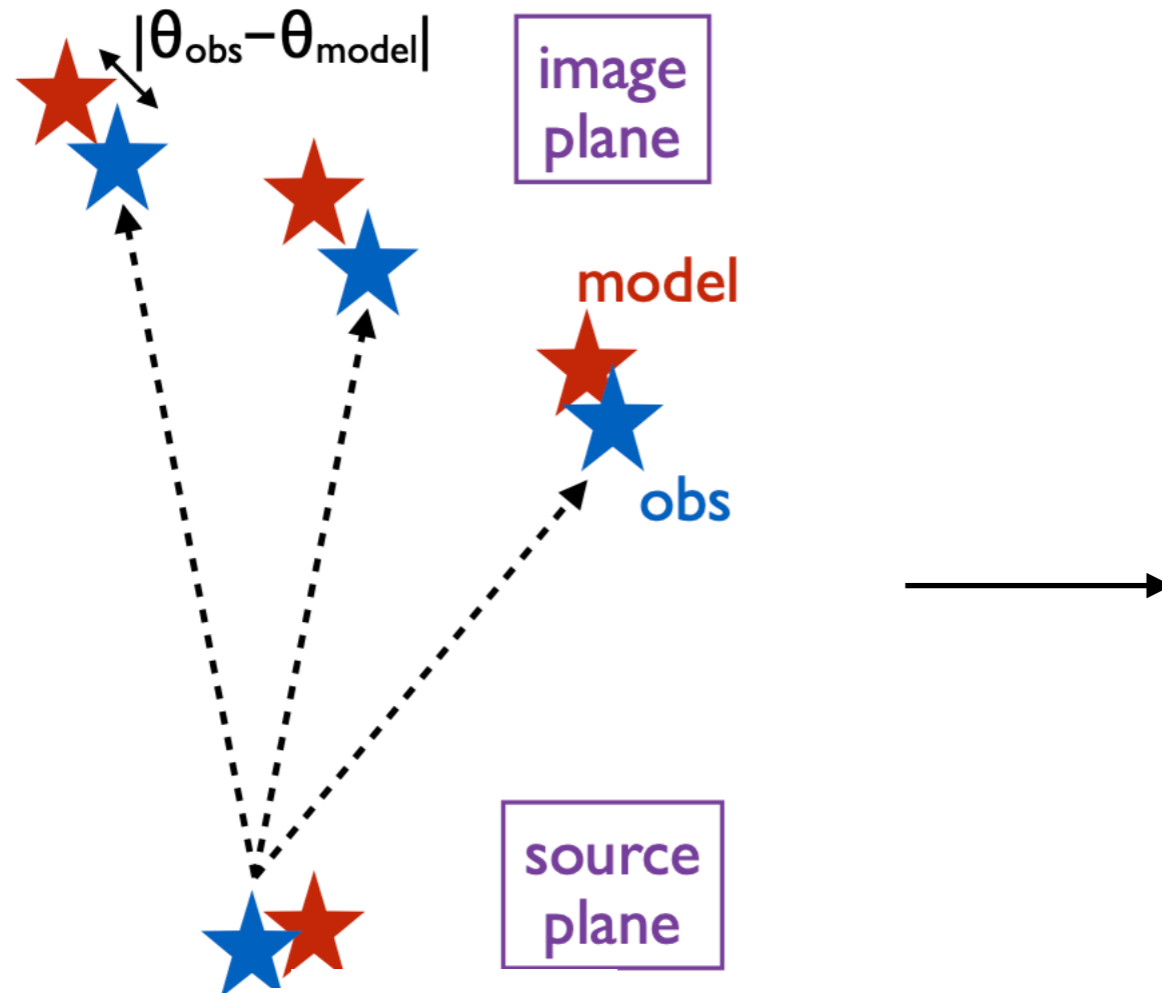


on magnification



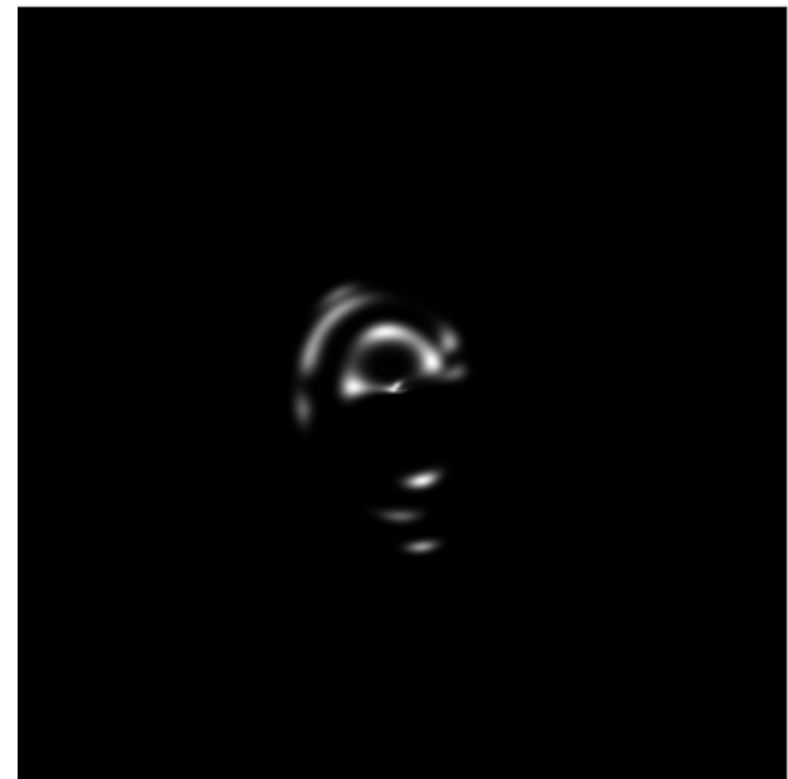
on cosmography

III. Solution: A pixelated method



$$\chi_{SL}^2 = \sum_{j=1}^{n_i} \frac{[x_{obs}^j - x^j]^2}{\sigma_{ij}^2}$$

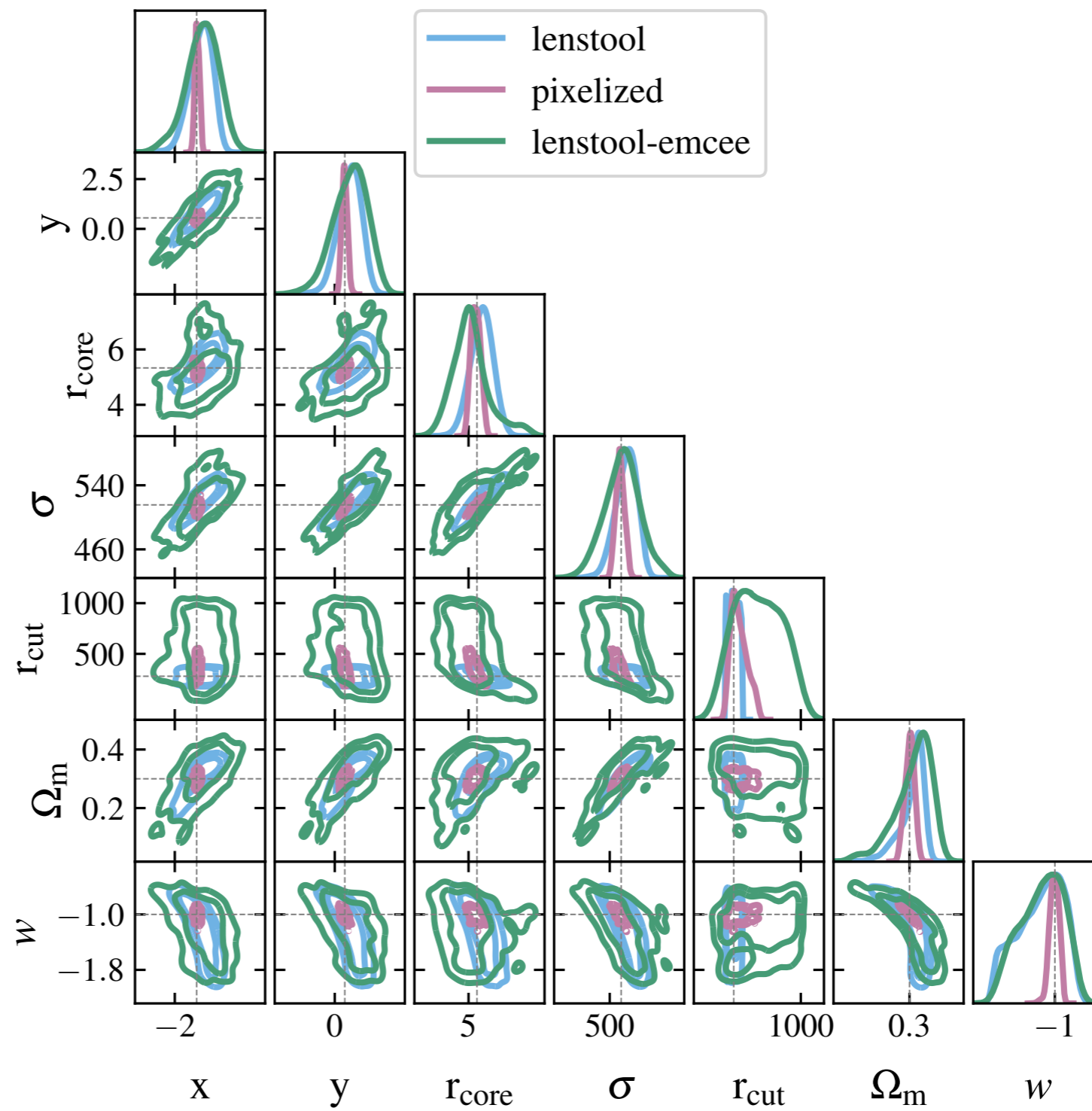
based on the extended surface brightness



$$\chi_{SL}^2 = \sum_{i=1}^{n_{pix}} \frac{[s_{obs}^i - s^i]^2}{\sigma_i^2}$$

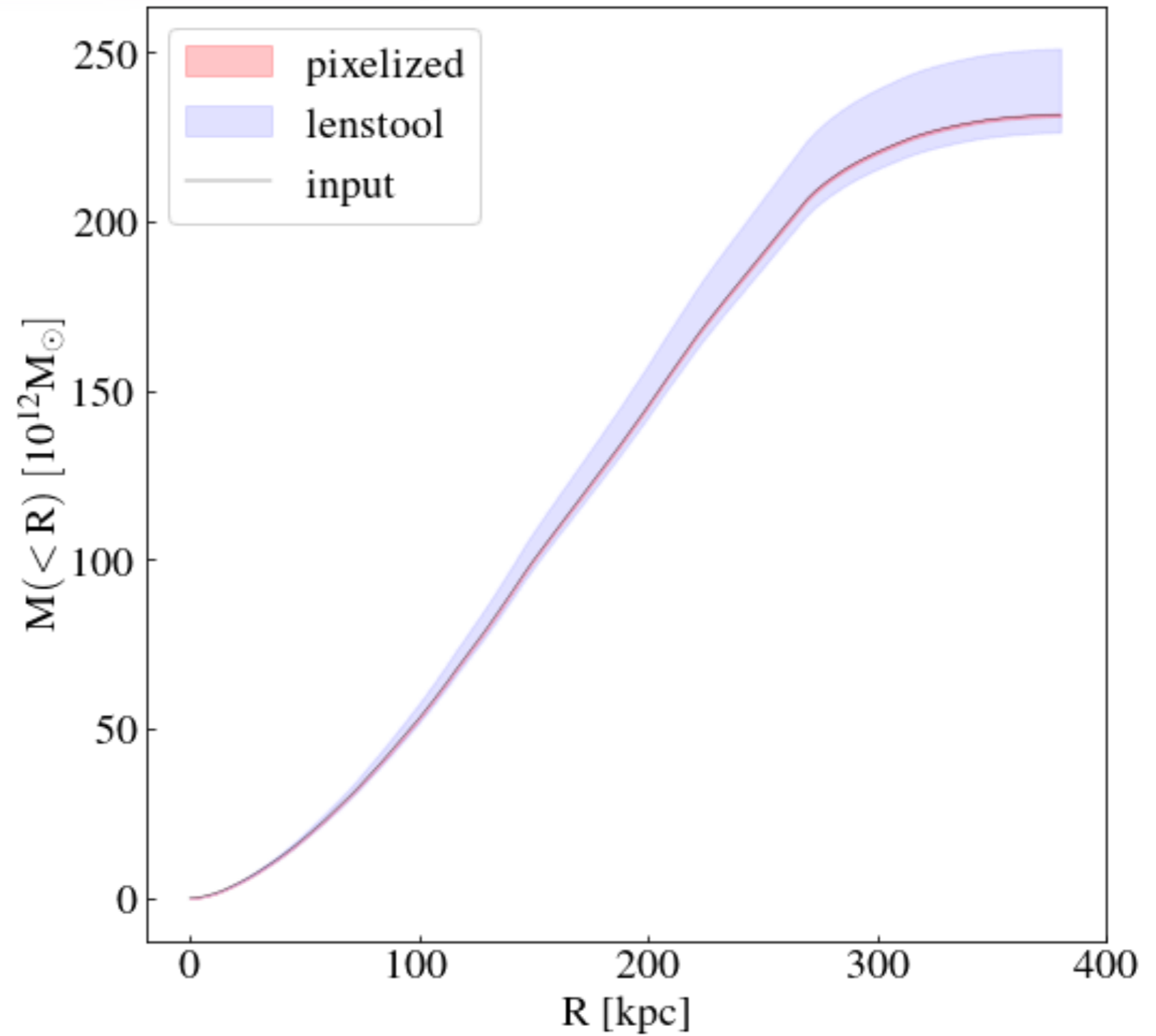
III. Solution: A pixelated method

Posterior

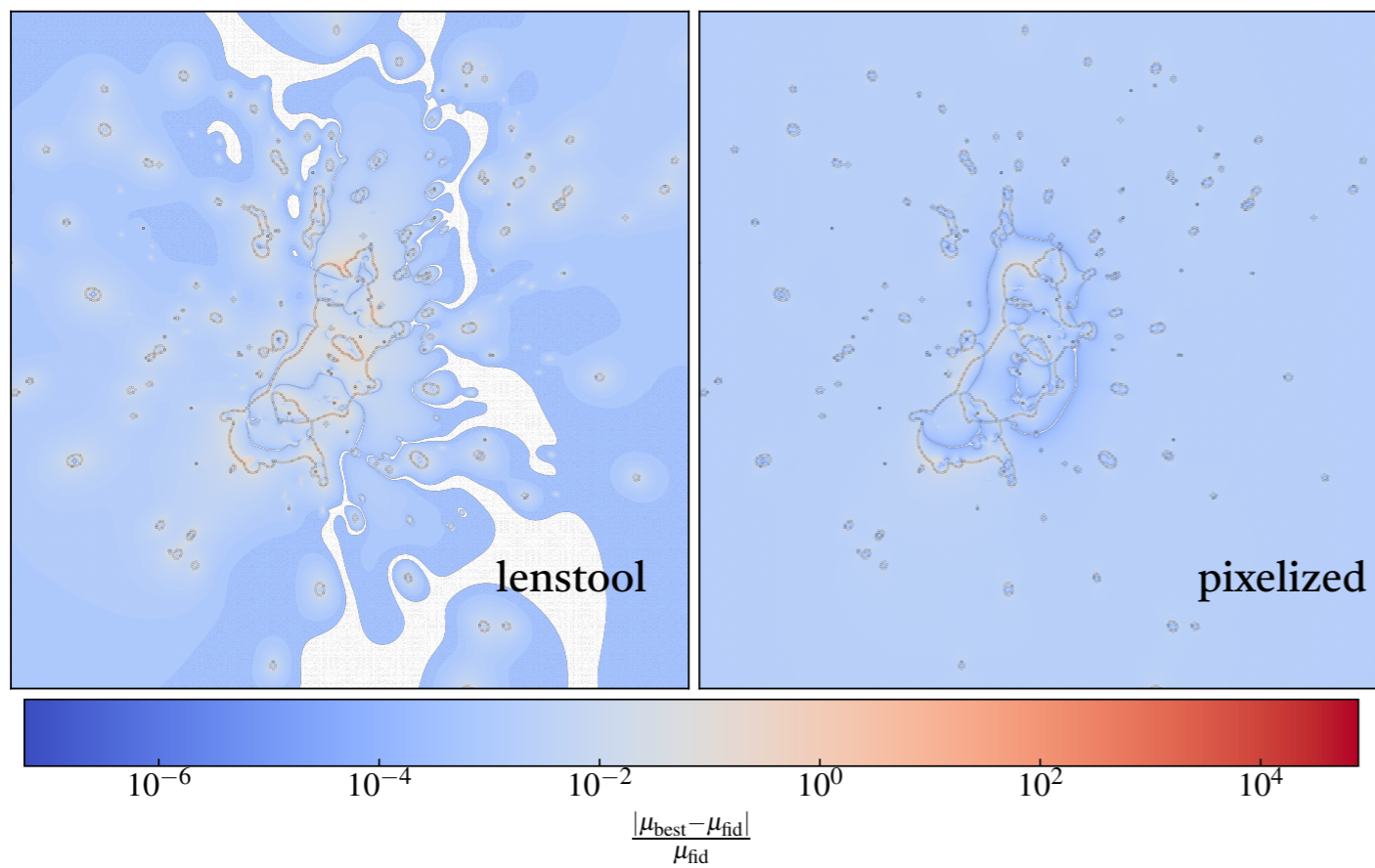


III. Solution: A pixelated method

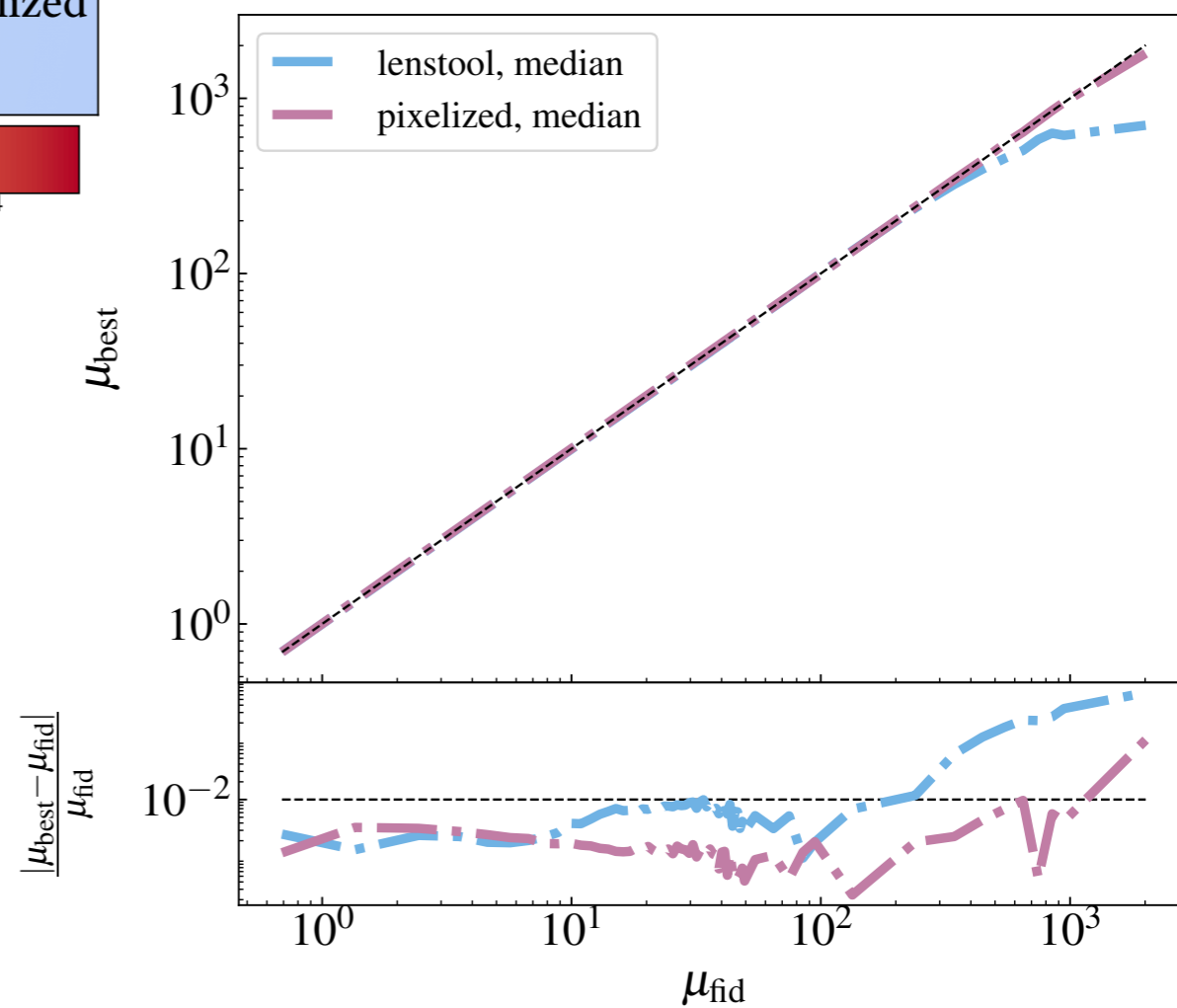
Cluster mass profile



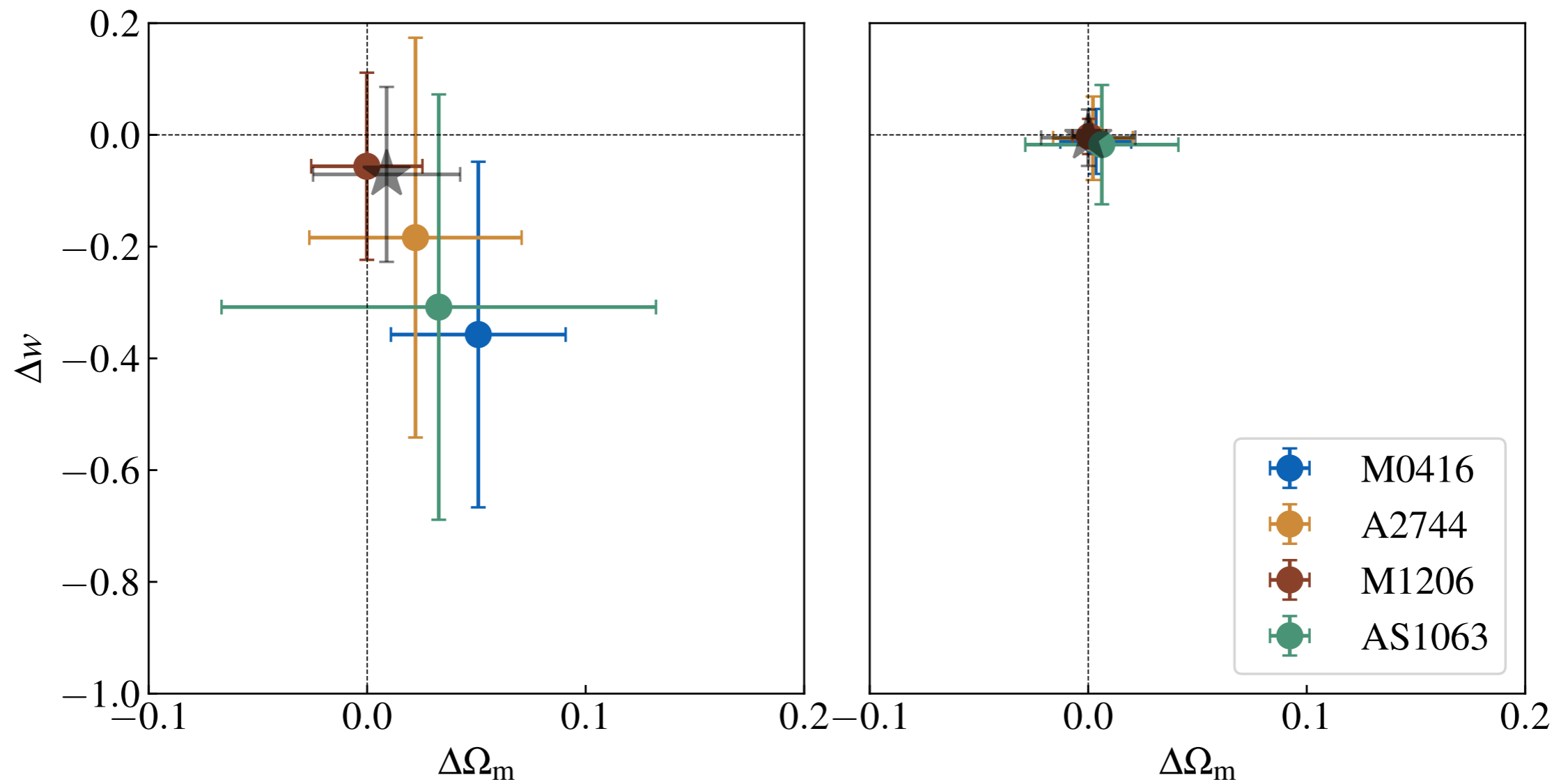
III. Solution: A pixelated method



Magnification maps



III. Solution: A pixelated method



Cosmological parameters

IV. Next step

“TOY”: analytical cluster mass

+ free parameters of only the main halo & cosmology

+ 3 image families as constraints

$\simeq 1$ day

Modeling:

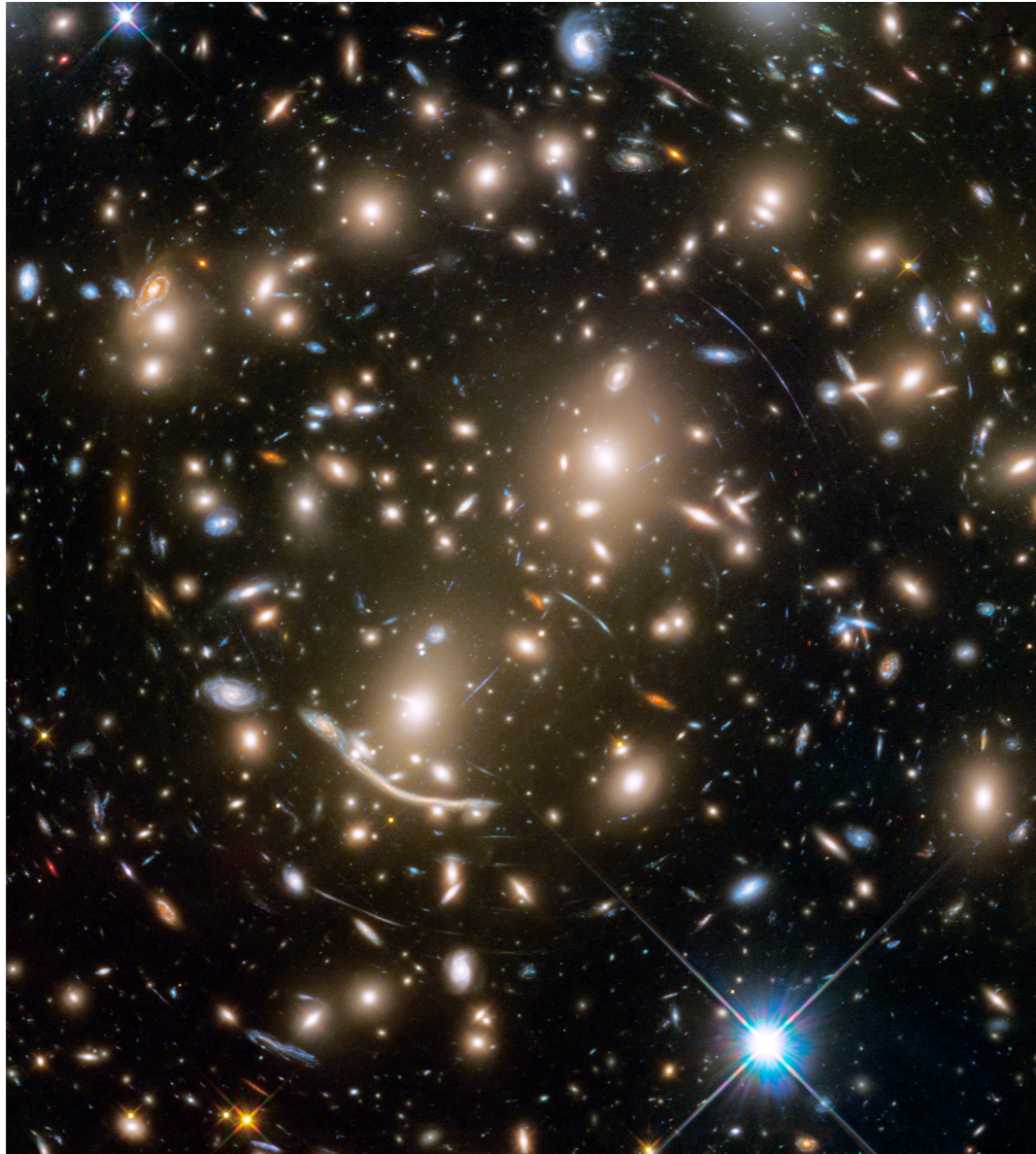
deflection angle map α \rightarrow de-lensing \rightarrow re-lensing \rightarrow sampling
JAX NumPyro

free the following 3 strong lensing parameters, and fix the other lensing parameters, as well as all the source parameters:

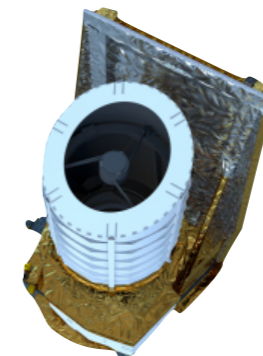
ELLIP:
PHIE:
VELDISP:

lib.	emcee	numpyro (0.12.1)	pymc
Device			
cpu ,4 cores (Jasm.)	> 1 h	14 min 01 s	1 min 51 s
Tesla T4 (google colab.)	/	10 min 08 s	
A100 (Jasm.)	/	1 min 03 s	

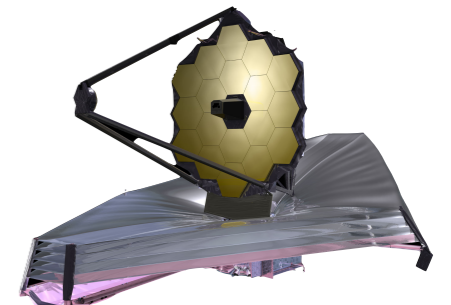
IV. Next step



CSST



Euclid



JWST

Apply on real SL clusters from the next-generation surveys

THANK YOU FOR
LISTENING!

